

6. This exercise is on  $\lambda \rightarrow$ -Curry.
- (i) Determine for each of the following terms (if typable) the most general type.

$$\lambda xy.x(yx),$$

**SII,**

**II.**

- (ii) Show that the terms  $\lambda xy.xy$  and **KI**( $\lambda x.xxx$ ) are not typable.
7. Investigate for each of the following  $\lambda$ -terms if it is typable in  $\lambda \rightarrow$ . If yes then give a type, if no then explain why not.

$$\lambda xy.x(\mathbf{I}x)y,$$

$$\lambda xy.x(x\mathbf{I})y.$$

8.  $\alpha$ ,  $\beta$  and  $\gamma$  are different typevariables.
- (i) Find inhabitants of
- $$(\alpha \rightarrow \beta \rightarrow \gamma) \rightarrow \beta \rightarrow \alpha \rightarrow \gamma$$
- $$(\alpha \rightarrow \alpha \rightarrow \beta) \rightarrow \alpha \rightarrow \beta$$
- $$(\alpha \rightarrow \alpha \rightarrow \beta) \rightarrow ((\alpha \rightarrow \beta) \rightarrow \gamma) \rightarrow \gamma.$$
- (ii) Prove that  $((\alpha \rightarrow \beta) \rightarrow \alpha) \rightarrow \alpha$  is not inhabited. You may use that each typable term has a normal form.
9. In untyped lambda calculus solve
- (i)  $Fx = x\mathbf{I}(\mathbf{K}x).$
- (ii)  $FxF = x\mathbf{I}(Fx).$
- (iii)  $Fx = x\mathbf{I}(Fx).$